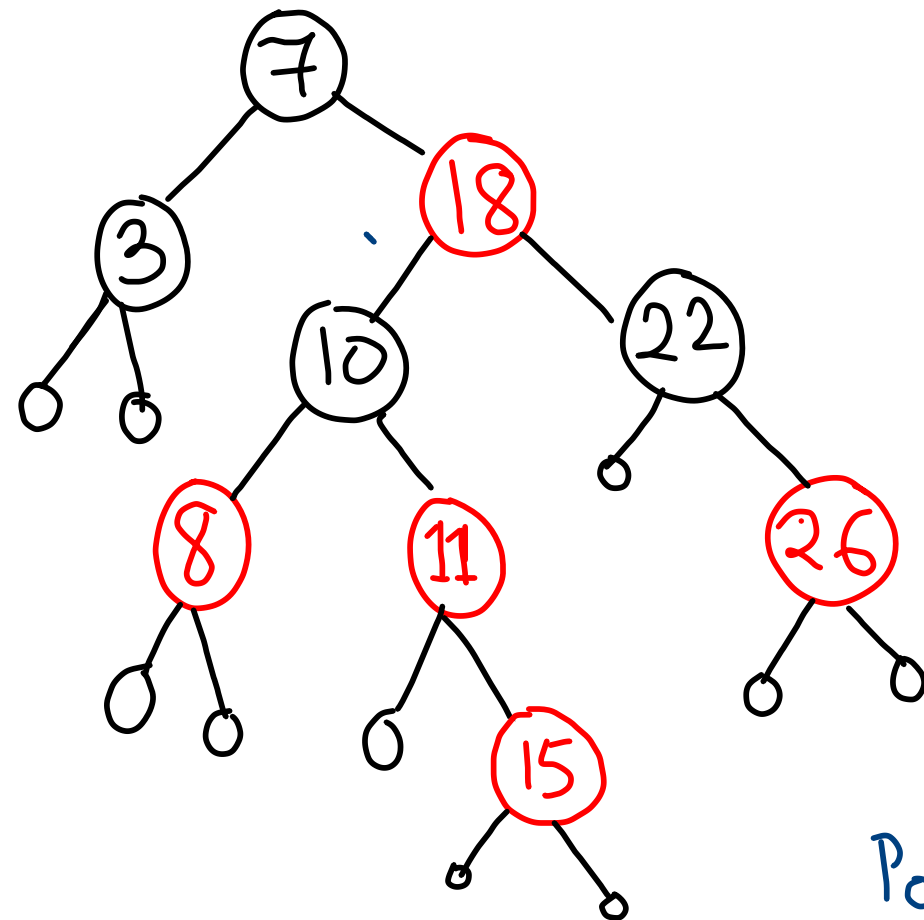
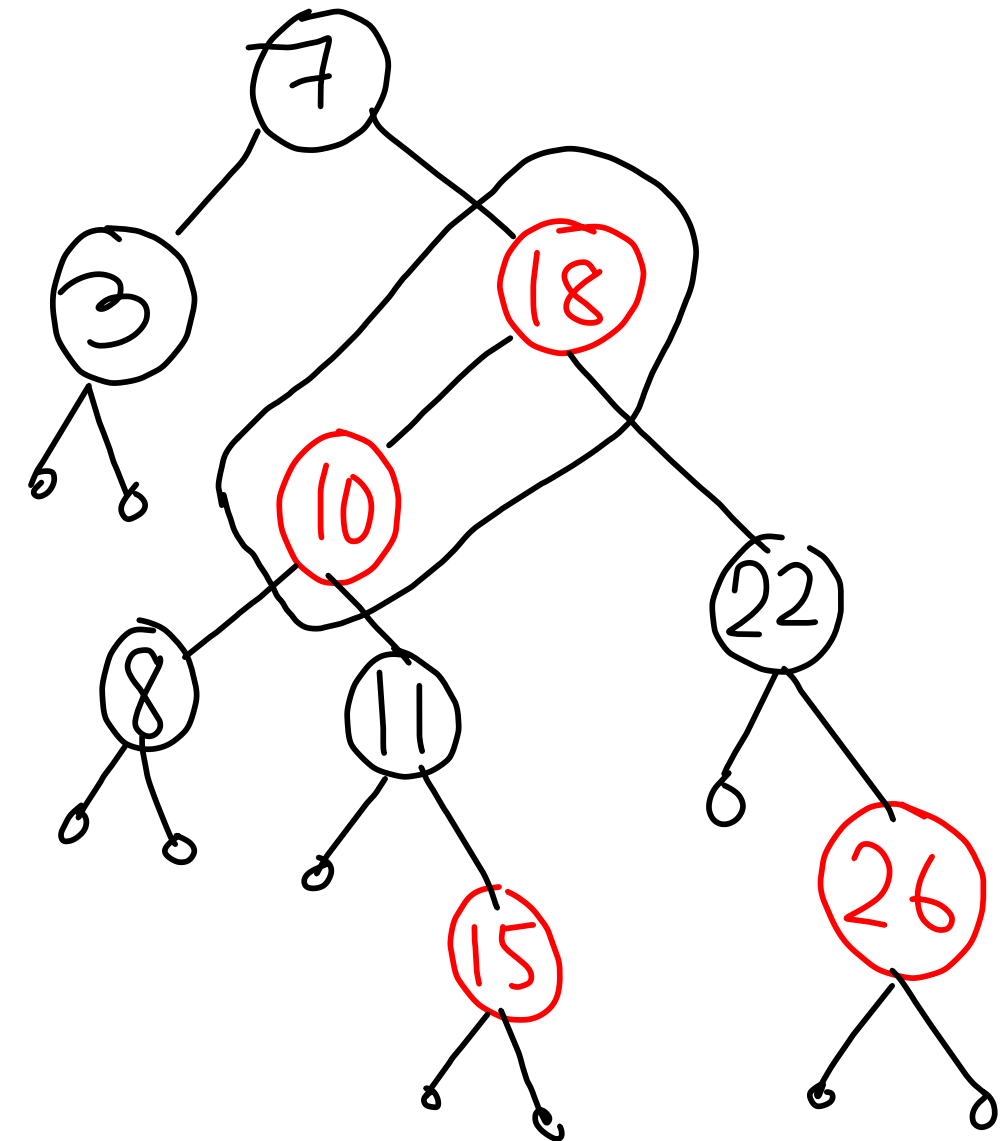
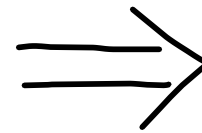


RED BLACK TREE : INSERTION



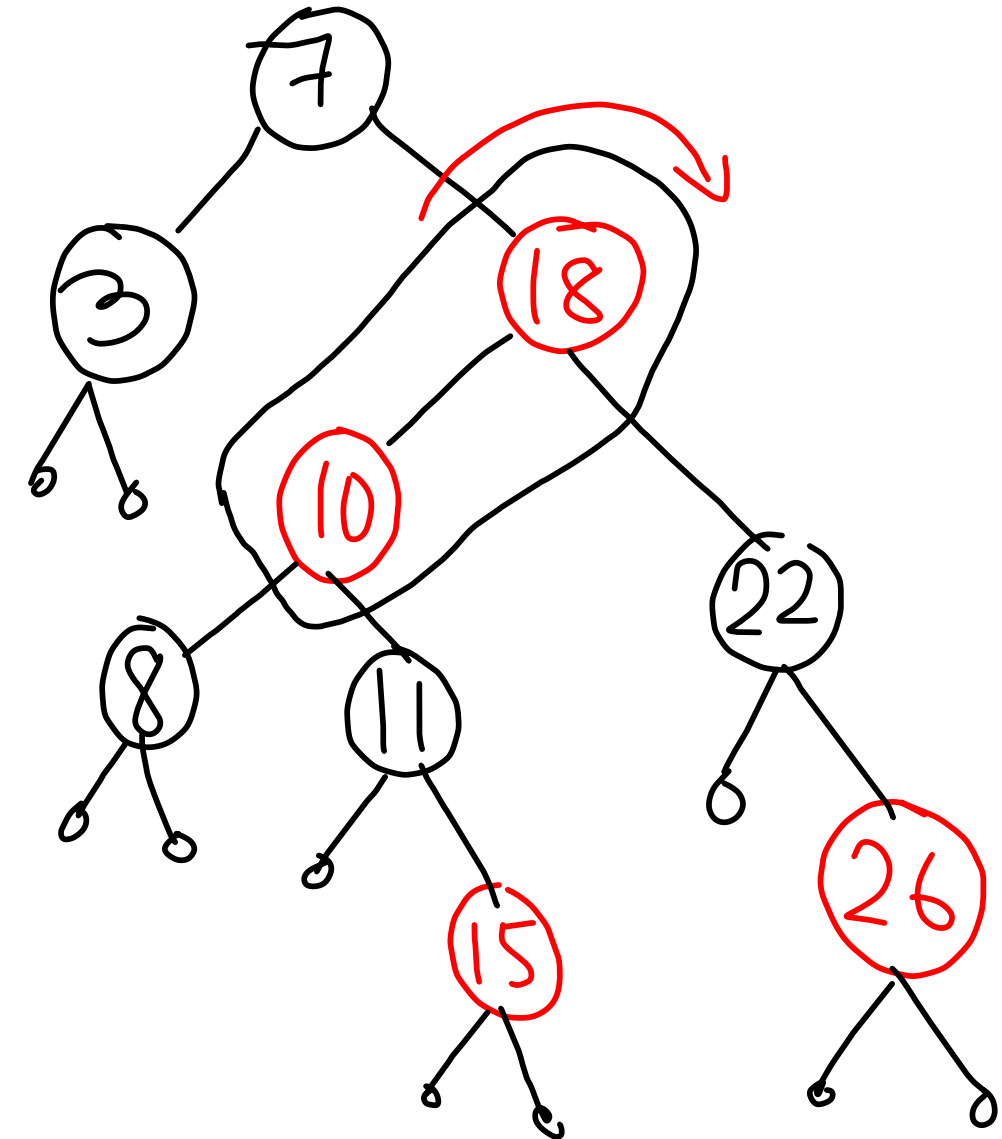
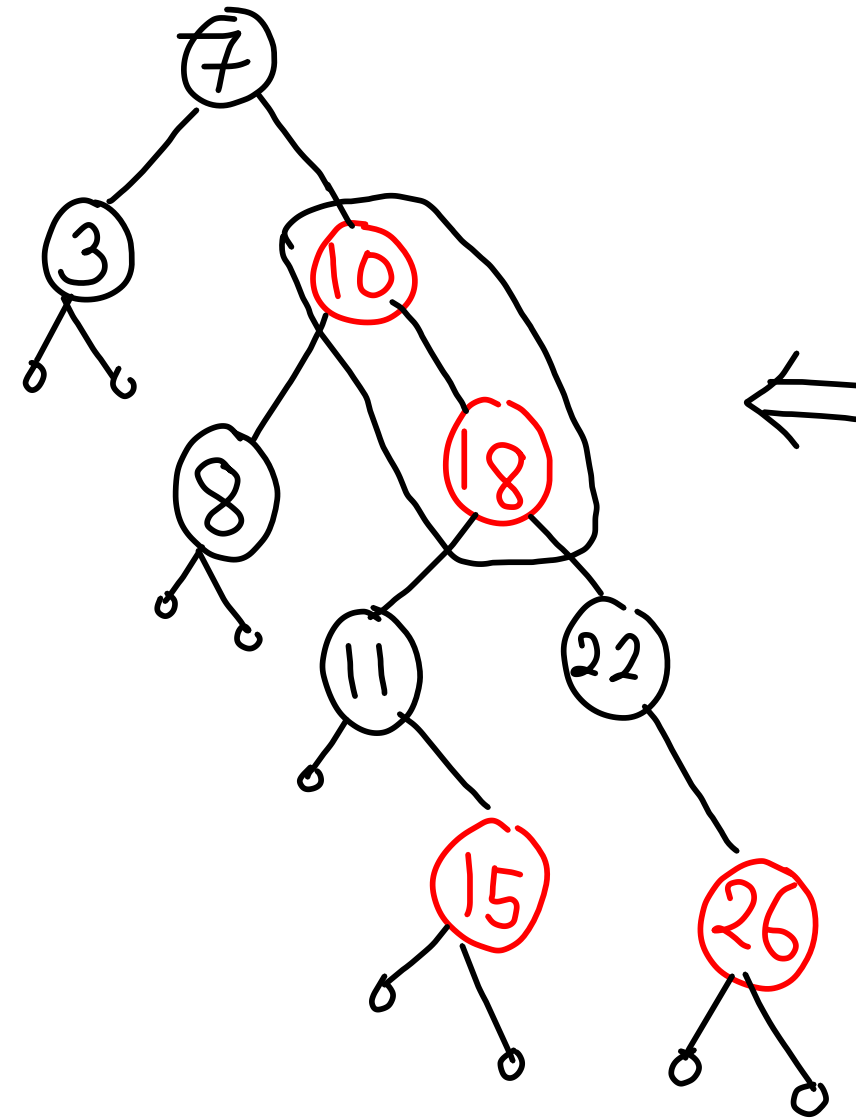
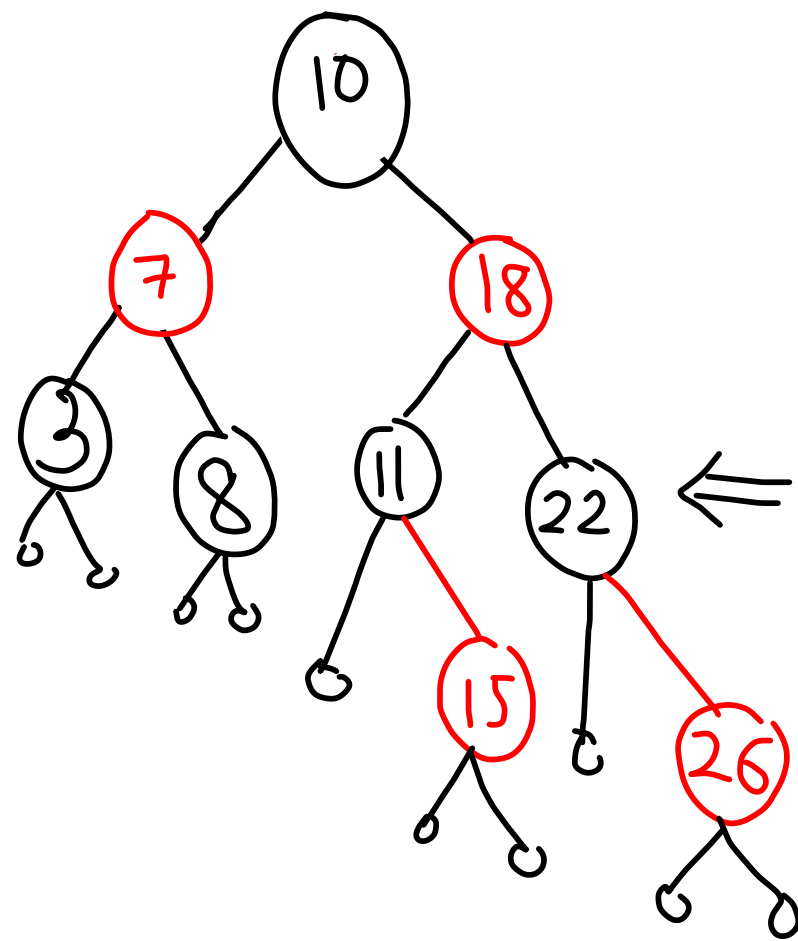
Insert "15"

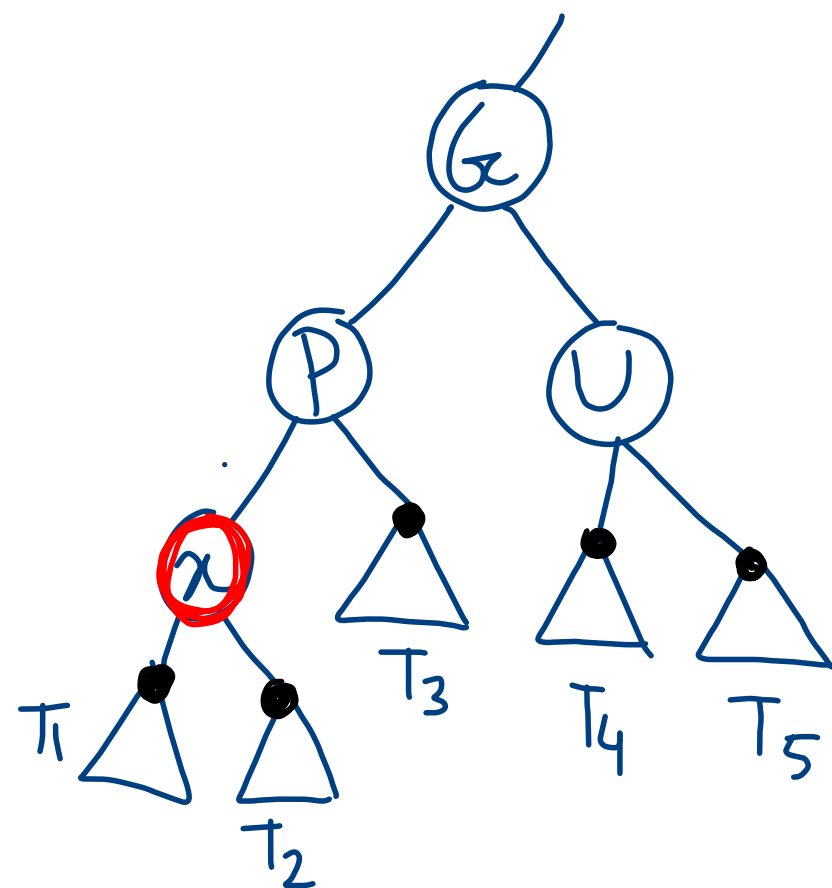


Possible Choices

- Recolor "15" to Black $\rightarrow$ Black height not satisfied
- Recolor "8" & "11"

RED BLACK TREE : INSERTION





Insert(x)

Case 1: P is black $\rightarrow$ Don't do anything.

Case 2: P is red

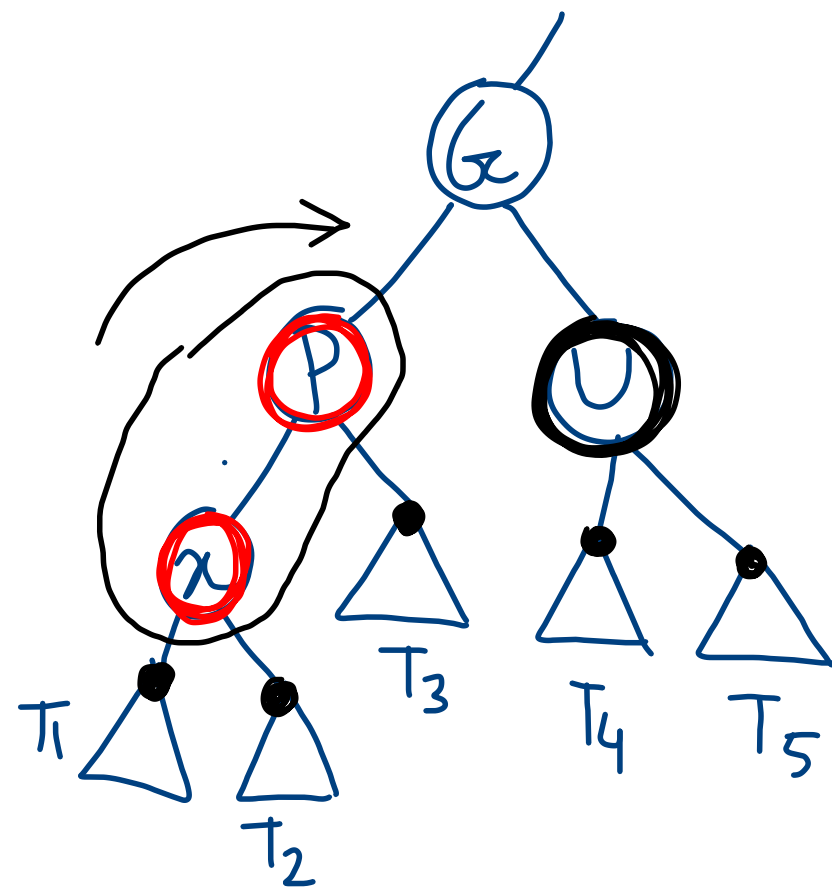
Subcase 2.a (U is red)

- L Recolor both P & U to black
- L Recolor G to red (to maintain black-height)
- L Recursive use the algo on G.

Subcase 2.b

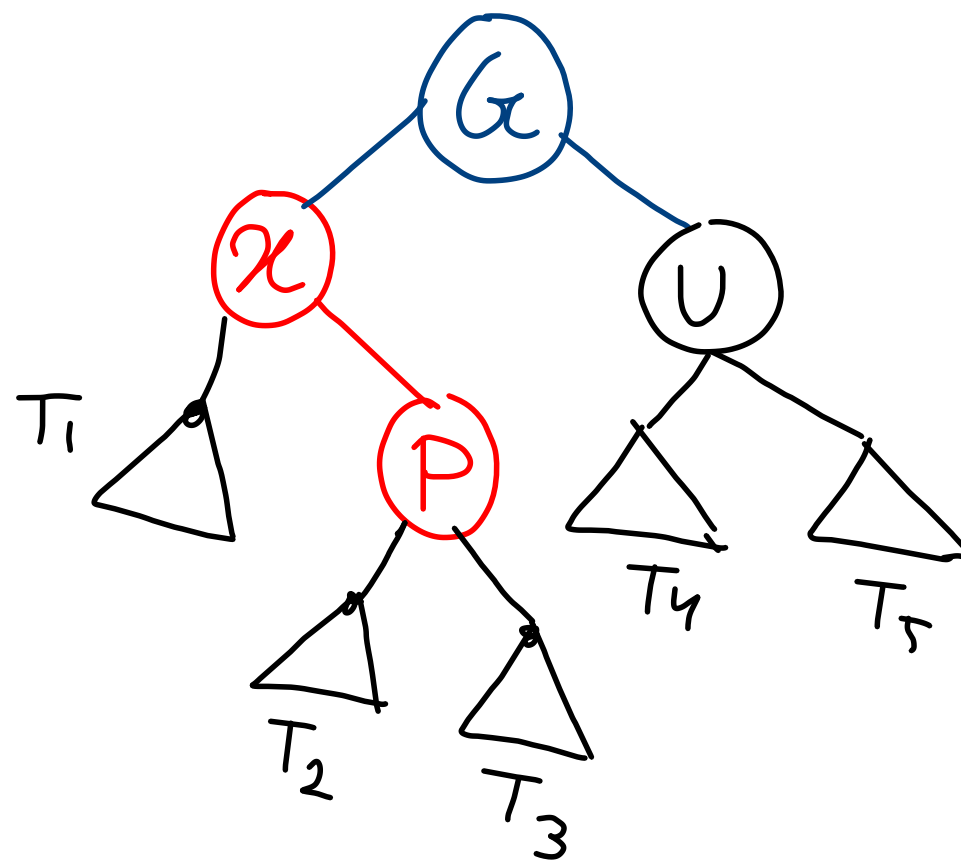
(U is black)

- L LL Config $\rightarrow$ 1 Rotation
- L LR Config $\rightarrow$ 2 Rotations
- L RL Config $\rightarrow$ 2 Rotations
- L RR Config $\rightarrow$ 1 Rotation



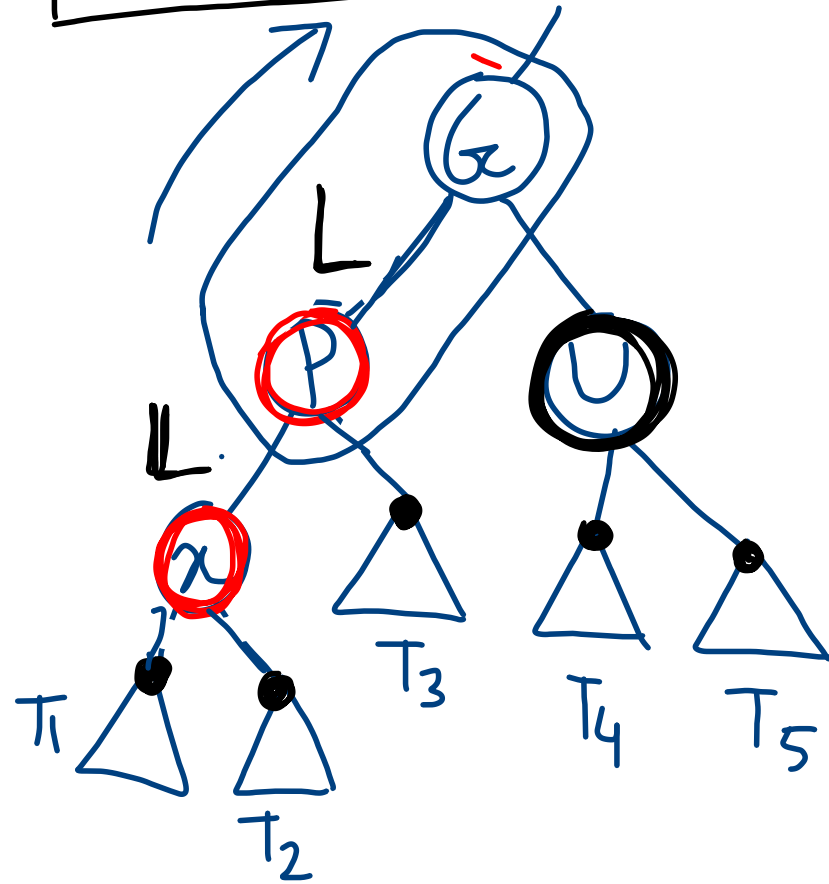
Insert(x)

P is Red, U is black



May not be a good
option due to black-height

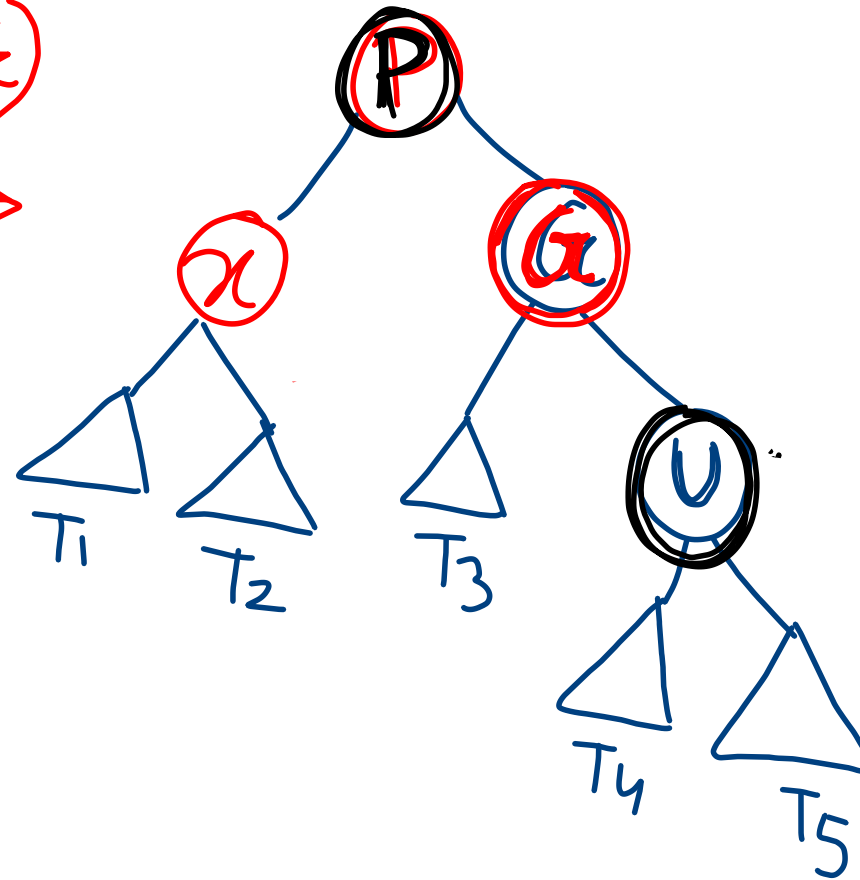
LL Structure



Insert(x)

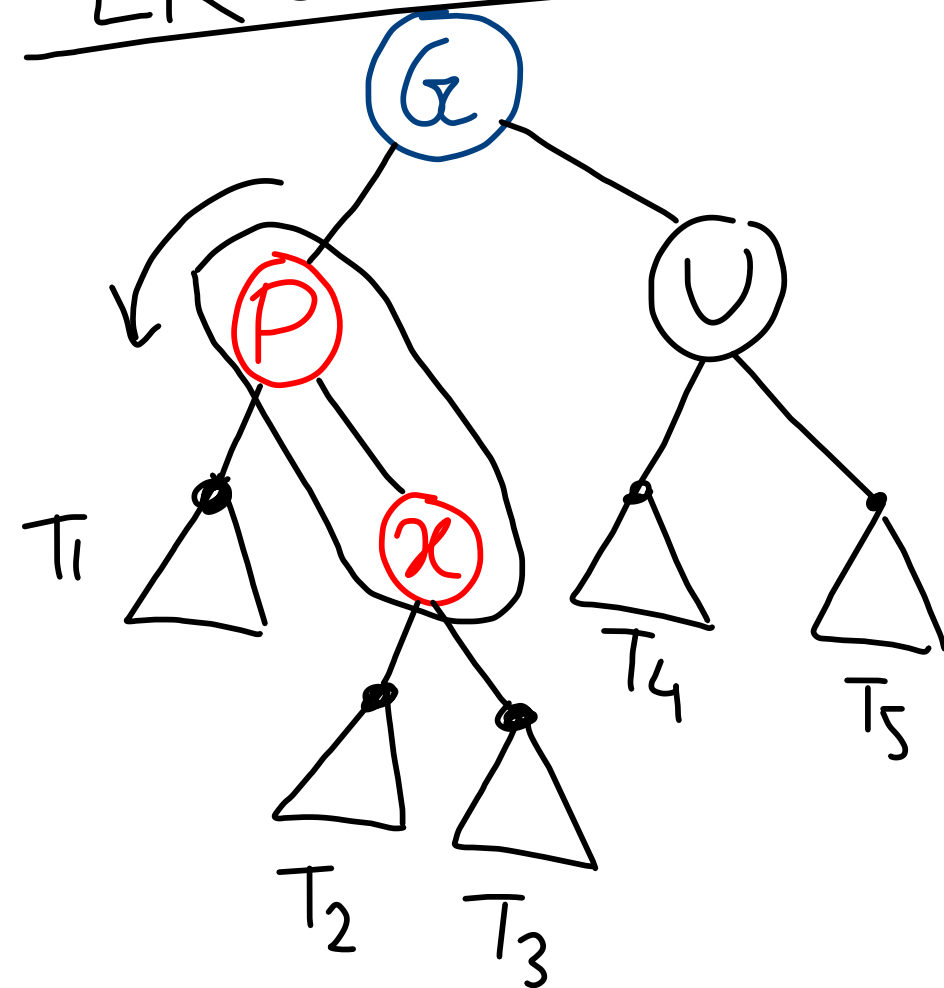
Right Rotate (G)
Swap Colors (P & G)

P is Red, U is black

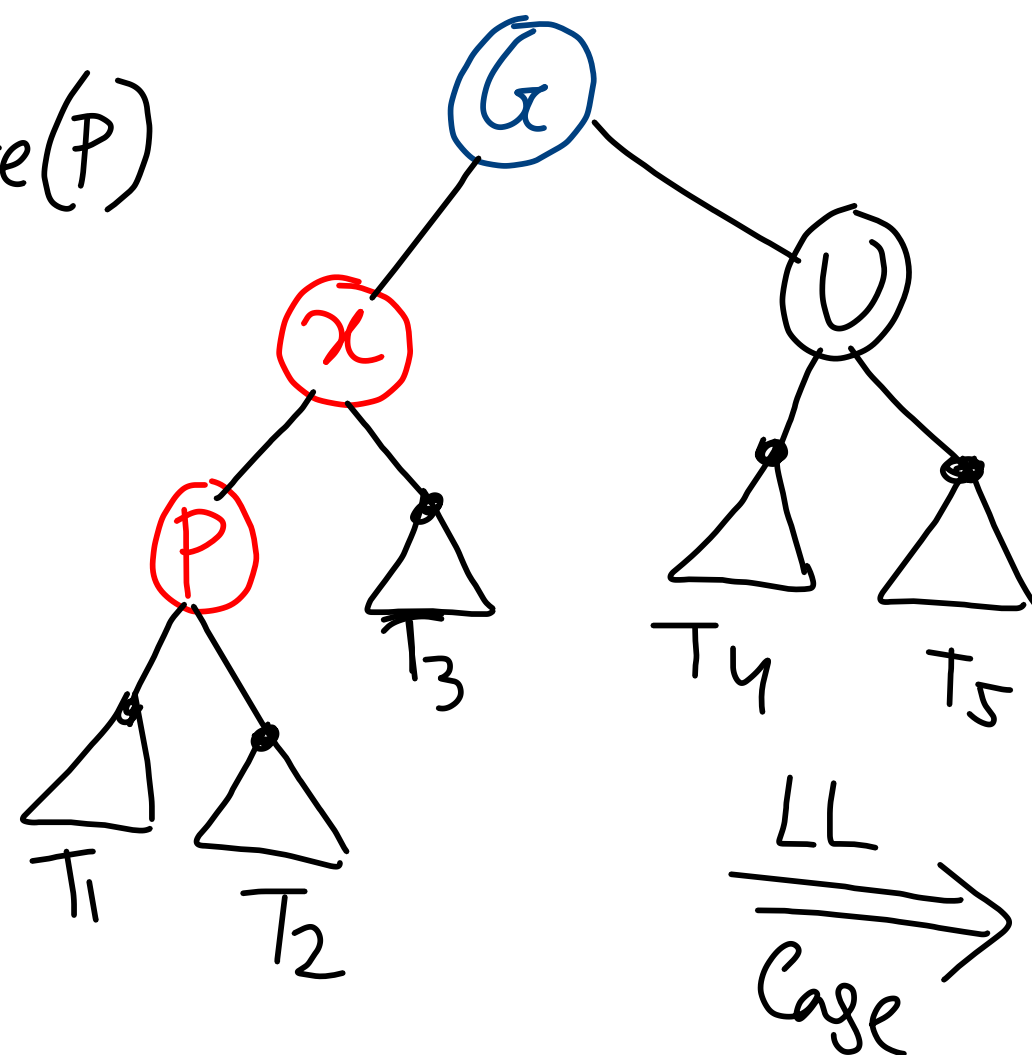


May not be a good
option due to black-height

LR configuration



LeftRotate(P)

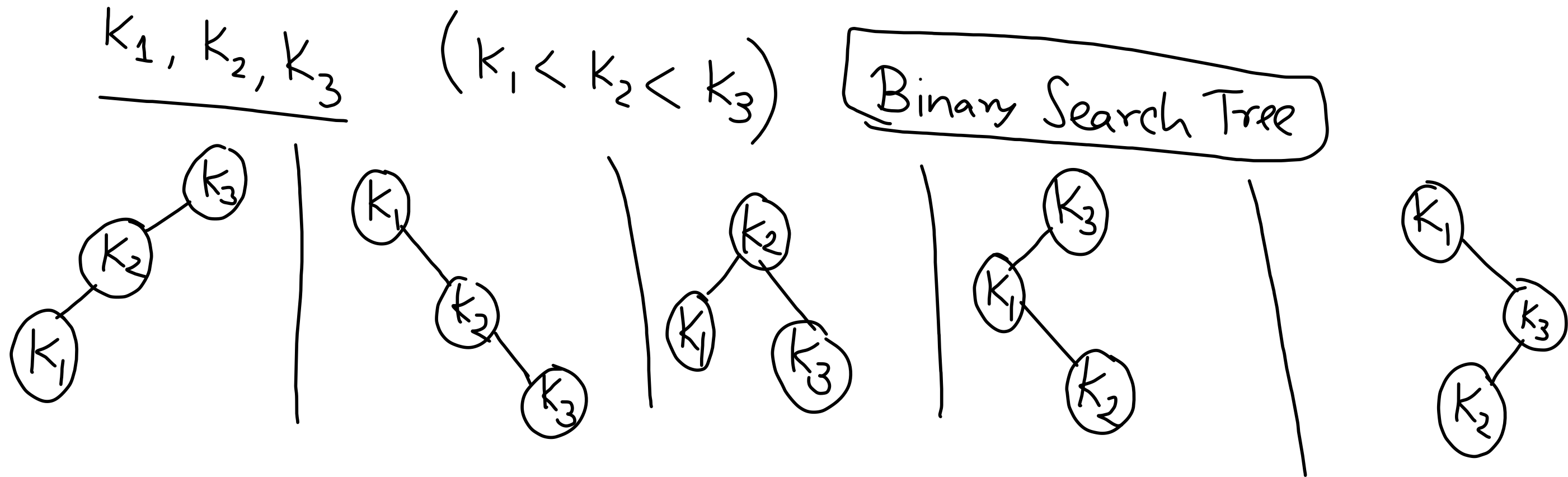


LL
Case

- You have a file F containing several words.
- You would like to search for some words (whether $w \in F$?)

Which Data Structure you should use?

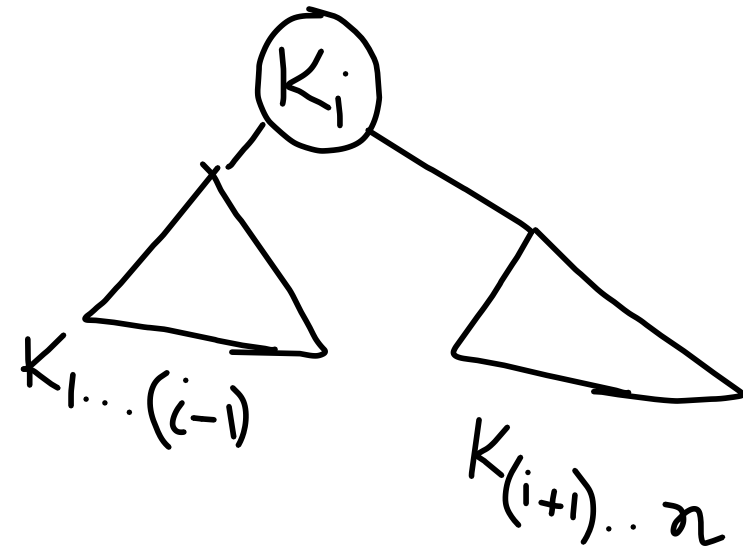
└ AVL / RBT (height balanced) — Searching time $O(\log n)$.



$n \rightarrow$ nodes

$$(k_1 < \dots < k_n)$$

How many binary Search-trees are there?



$$T(n) = \sum_{i=1}^n T(i-1) \cdot T(n-i)$$

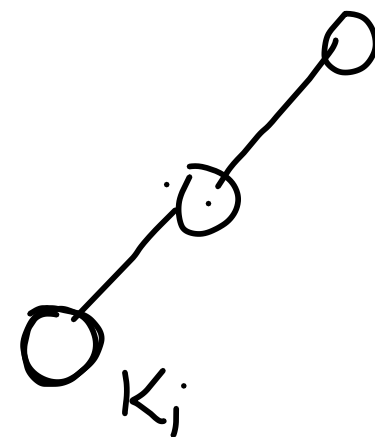
$$= \frac{(2n)!}{(n+1)! n!}$$

$\hookrightarrow$ exponential

$k_1, \dots, k_n$ ($k_1 < \dots < k_n$)

$w_1, \dots, w_n$ (weights)

$h=2$



Goal: Minimize

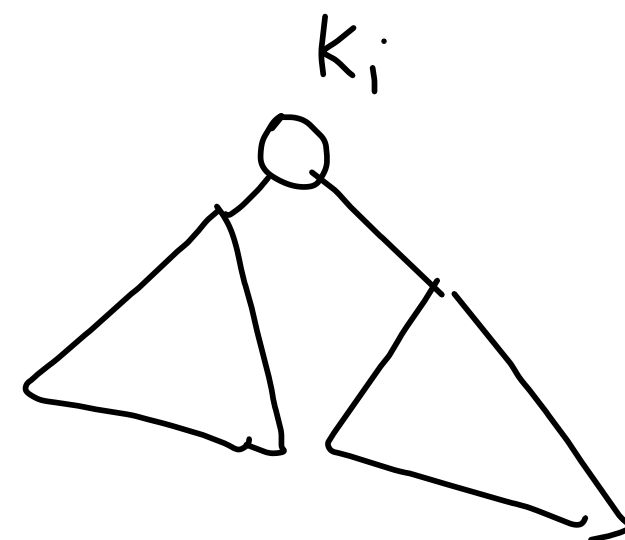
$$\sum_{i=1}^n (\text{height of } (k_i) + 1) \cdot w_i$$

$(\text{height of } (k_i) + 1) \cdot w_i$

- Exponential - (Trivial)

- Greedy Algo -

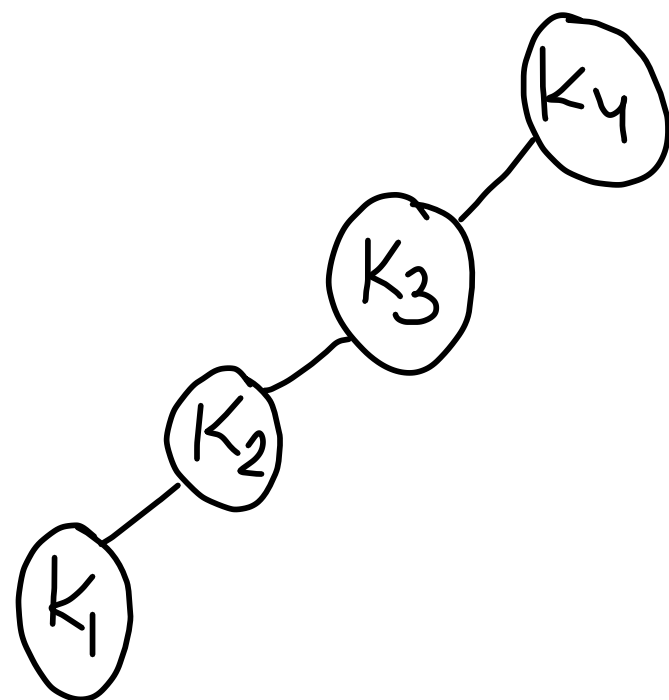
- Put most frequent on top
- Recursive use the algo.



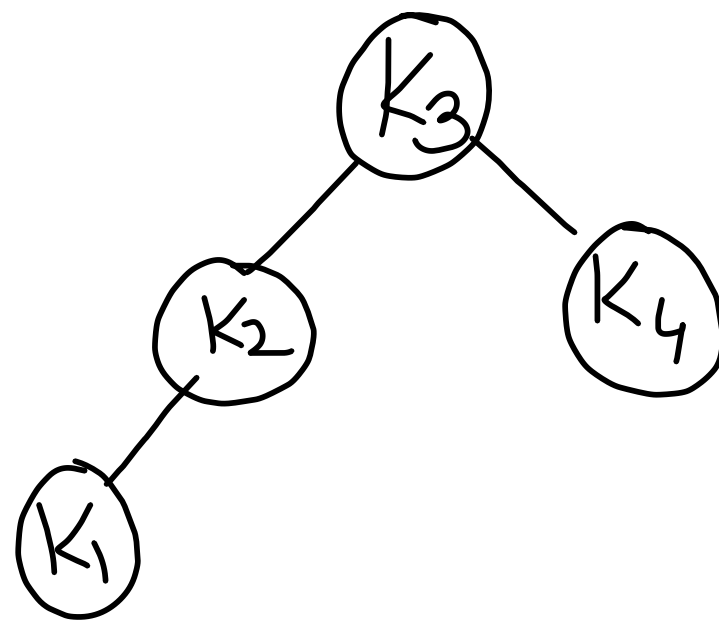
K_1, K_2, K_3, K_4

↓

1 8 9 10

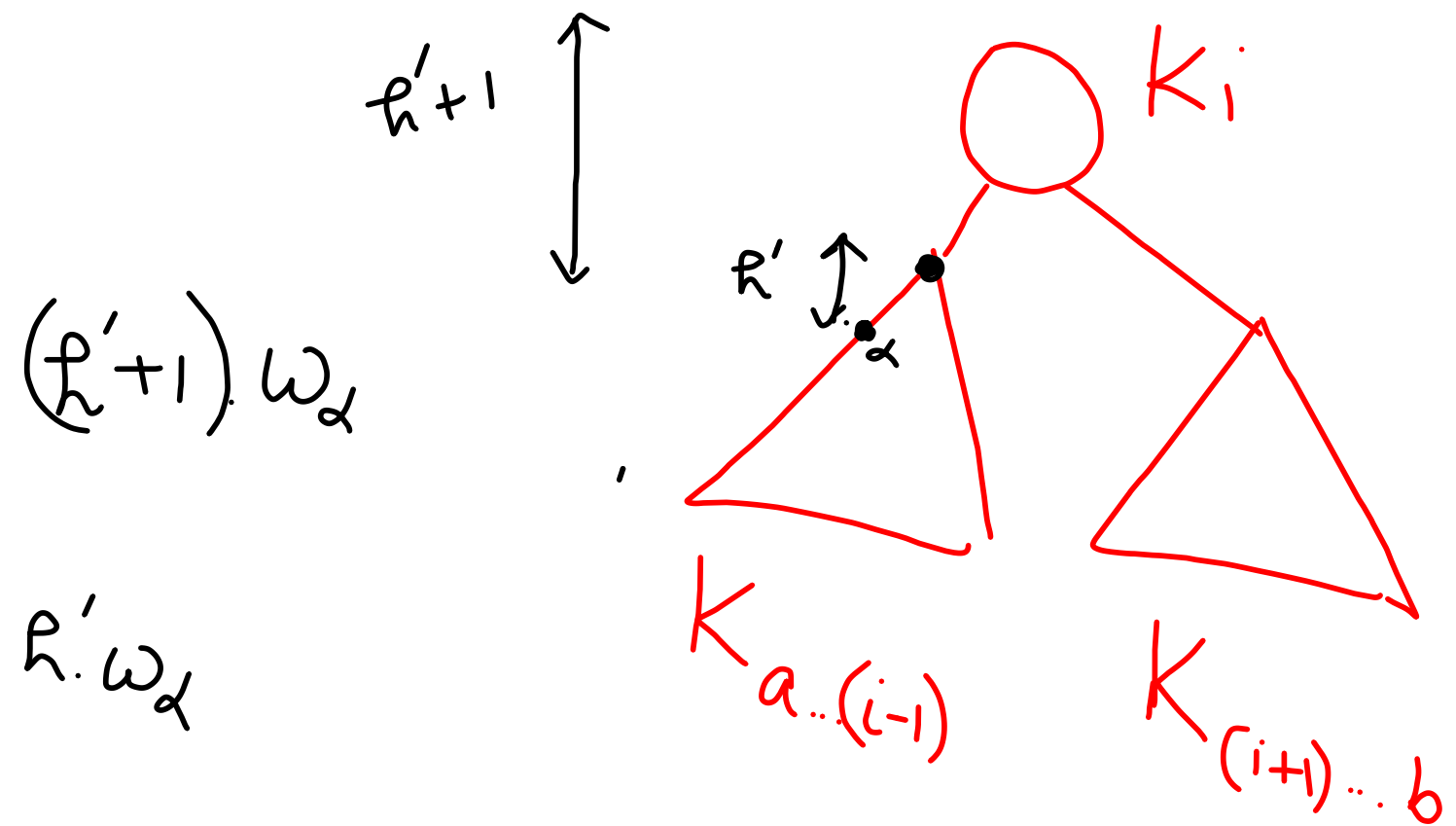


$$10 \cdot 1 + 9 \cdot 2 + 8 \cdot 3 + 1 \cdot 4 = 56$$



$$1 \cdot 3 + 2 \cdot 8 + 1 \cdot 9 + 10 \cdot 2 = 48$$

Dynamic Prog



$$e(a, b) = \begin{cases} w_i, & \text{if } a = b \\ \min_{a < i < b} \left\{ e(a, i-1) + e(i+1, b) + \sum_{j=a}^b w_j \right\} \end{cases}$$